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This ends the proof of Theorem 8.

Obvious examples show that the restriction $\lambda_i \leq 1$ in Theorem 8 may not be omitted.

Remark 6. It is easily seen that Theorem 8 is valid also if the circle C is not assumed to be *strictly* convex and smooth. The argument is completely elementary but somewhat lengthy, and we omit it. On the other hand, Theorems 1 qnd 2 have to be properly reformulated in order to be applicable (and valid) for circles which are not strictly convex and smooth.

Remark 7. It is easily seen that Theorems 1 and 2 do not generalize to higher-dimensional spaces. Theorem 8 is probably valid for spaces of any dimension (with $n + 1$ " solid " spheres covering the surface of another one in the n-dimensional case), although no proof seems to be known even in the case of Euclidean spheres in three-dimensional space.

Note. After the present note was completed, the paper " Zur elementaren Dreicksgeometrie in der komplexen Ebene " (*Enseign. Math.*, *4* (1958), 178-211), by J. E. Hofmann, came to our attention. In this paper the geometry of triangles in the Euclidean plane is developed (in part) in a way closely related to the method used in the present paper.

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